

# Physics based scour model applied to Tucuruí Dam (Brazil)

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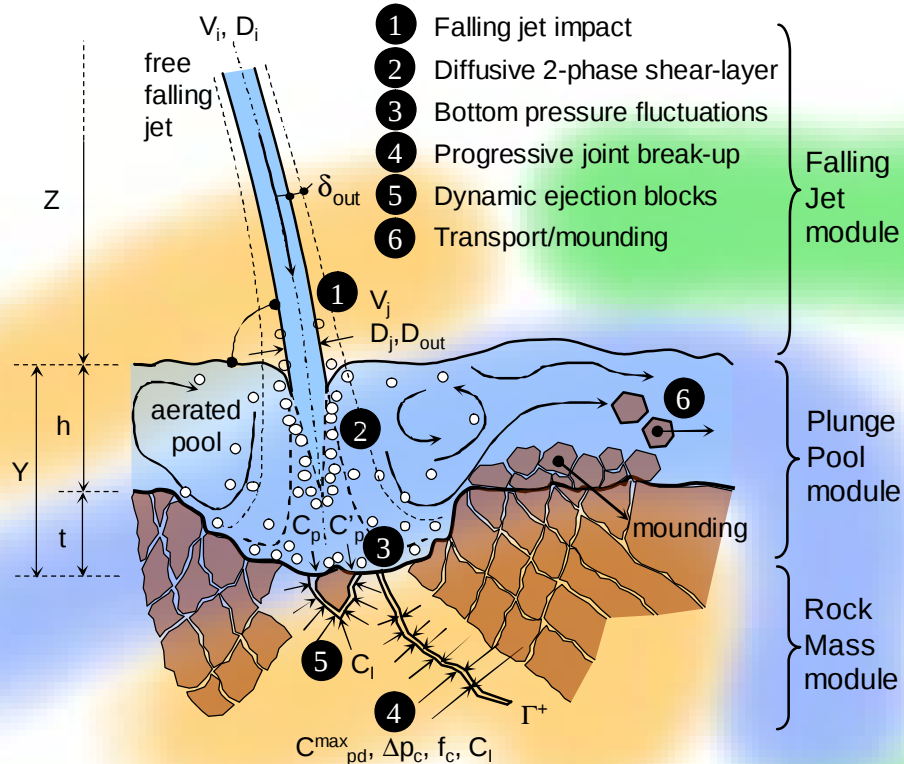
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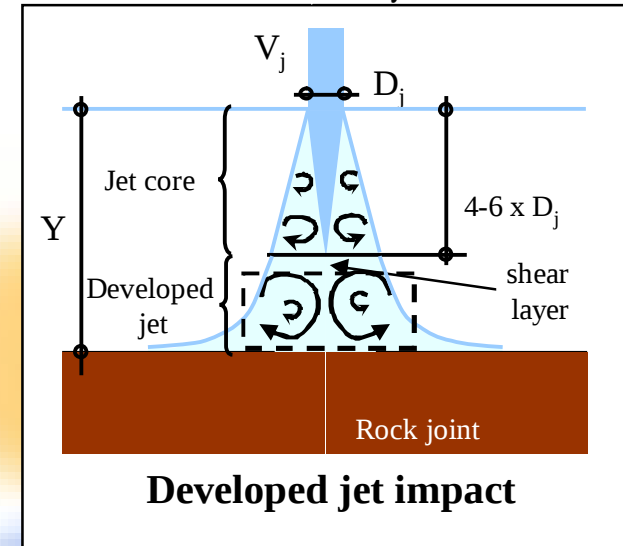
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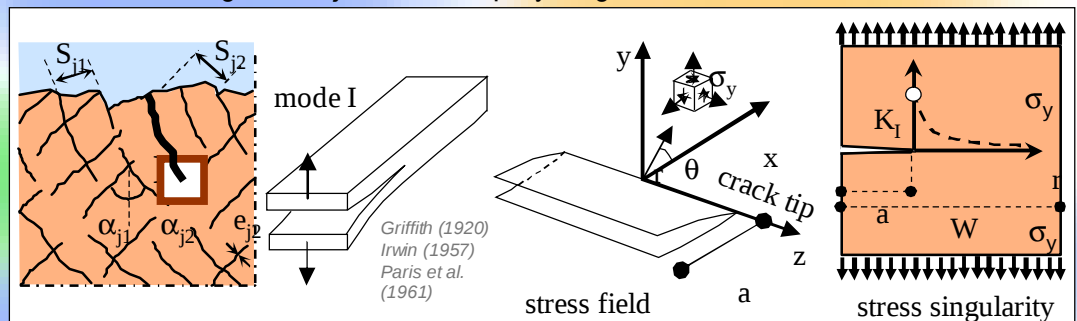
## Physical-mechanical processes



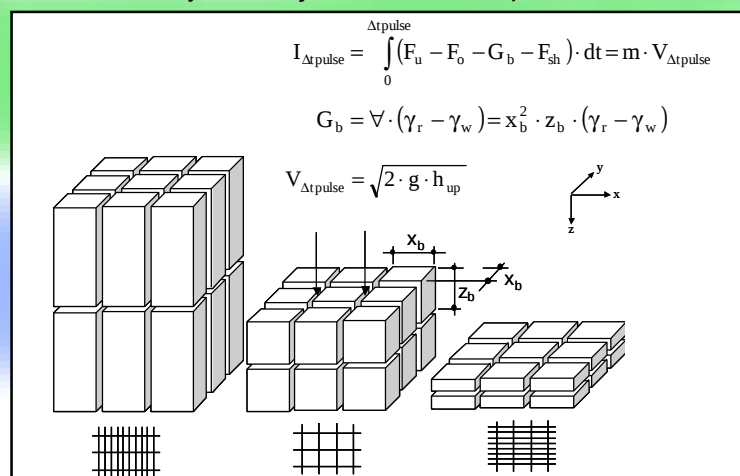
## Process 2. Diffusive shear layer: Jet module



## Process 4. Progressive joint break-up by fatigue: LEFM model



## Process 5. Dynamic ejection blocks: Uplift model



$$\sigma_{ij} = \frac{K_I}{\sqrt{2\pi r}} \cdot f_{ij}(\theta) + \text{higher order terms}$$

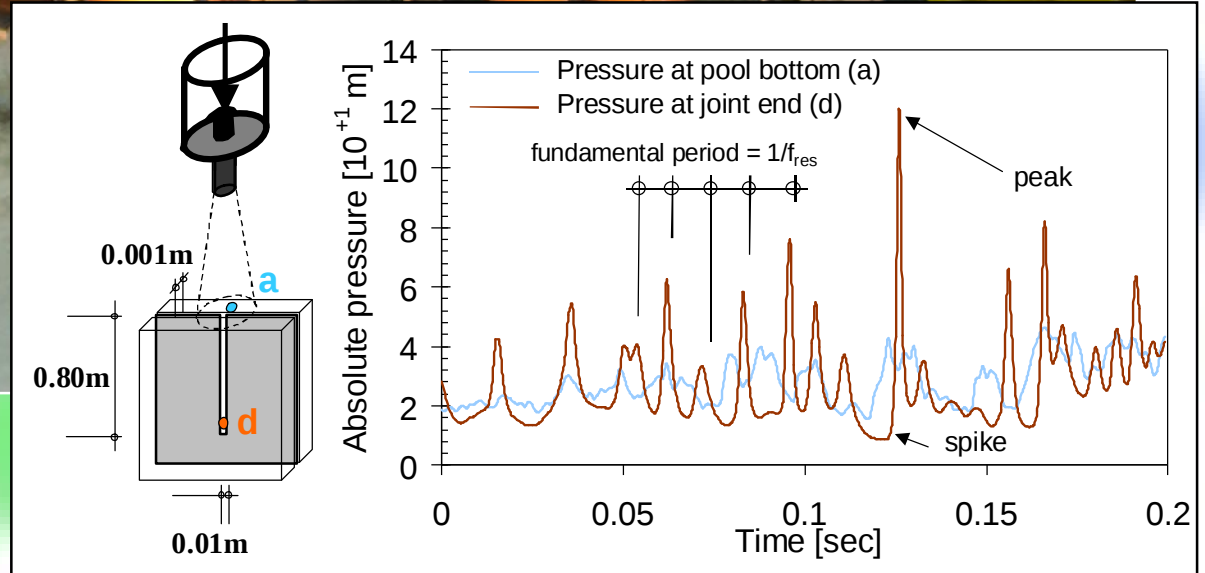
$$K_I = \sigma_{max} \cdot \sqrt{\pi \cdot a} \cdot f\left(\frac{a}{W}\right)$$

$$\Delta a_c = \int_0^{t_f} (f \cdot C \cdot S_{max}^m \cdot S_a^n + v \cdot e^{bs}) \cdot dt$$

- $K_I$  = f (pressure distribution)
- $K_I$  = f (in-situ stress field)
- $K_{Idyn}$  = f (pressurization rate)
- $f(a/W)$  = f (geometry fissure) planar, ...
- $K_{Ic}$  = fracture toughness value
  - literature
  - tests

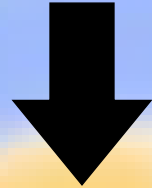
Grady & Kipp (1980)  
Haimson & Zhao (1991)  
Zhao & Li (2000)  
Zhao (2000)  
Zhang et al. (2000)

(after Costin & Holcomb 1981)





- use of dynamic pressures at plunge pool bottoms
- computation of transient pressures inside rock mass
- comparison with resistance of rock mass against fracturing
- computation of net uplift pressures on single rock blocks
- comparison with resistance of blocks against uplift

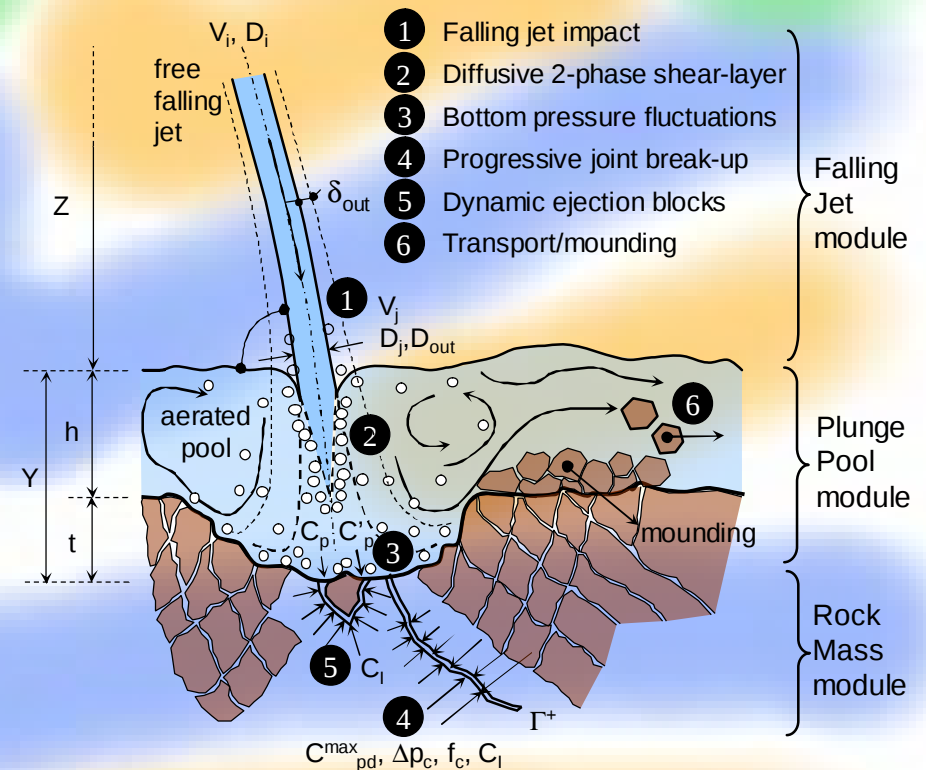


**New engineering model  
 for evaluation of ultimate scour  
 and time evolution of scour formation**

## Modules:

1. falling jet
2. plunge pool
3. rock mass

- hydrodynamic forces in rock
- resistance criteria of fractured rock



## Falling jet

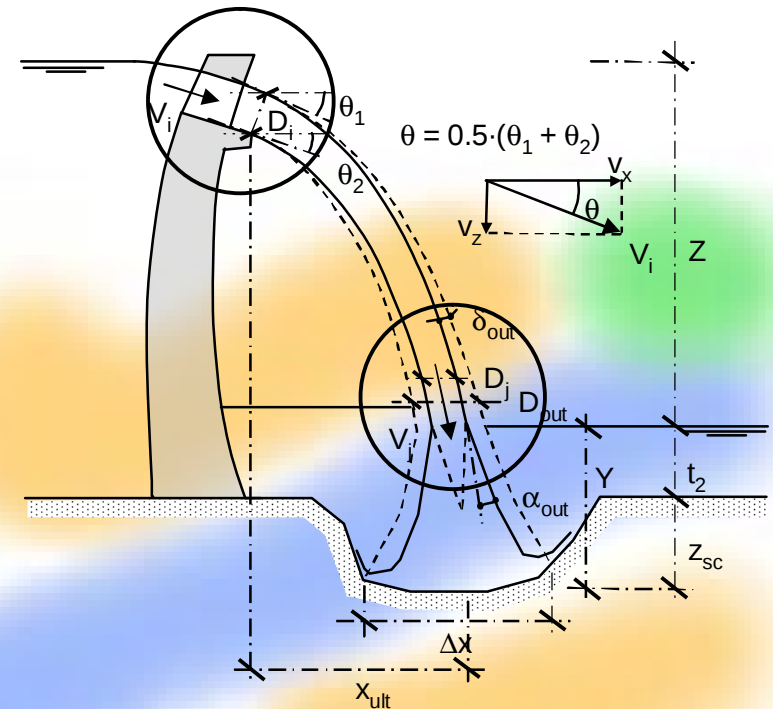
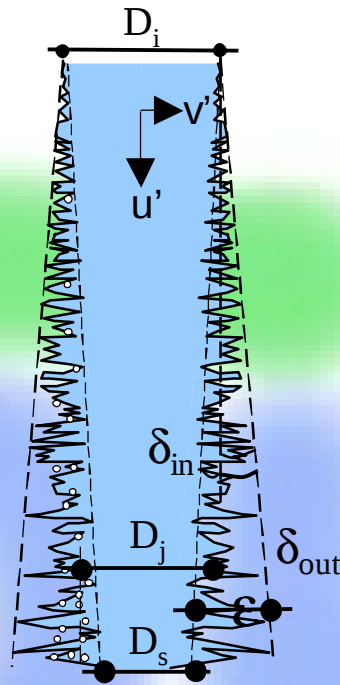
$$D_j = D_i \cdot \sqrt{\frac{V_i}{V_j}}$$

$$D_{out} = D_i + 2 \cdot \delta_{out} \cdot L$$

$$\delta_{in} = 0.5-1 \%$$

$$\delta_{out} = 3-4 \%$$

$$\delta_{out} \propto Tu$$

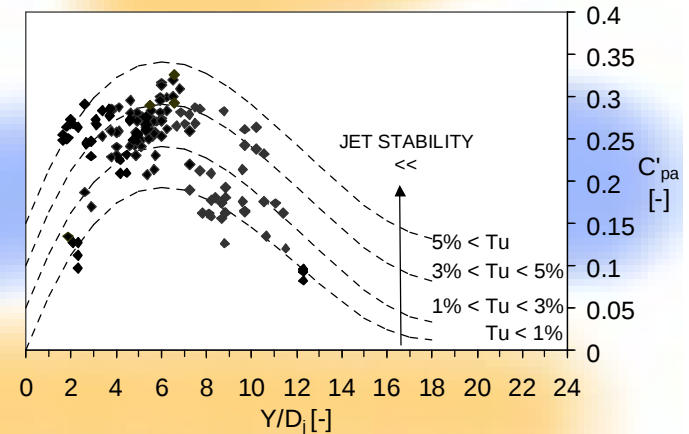
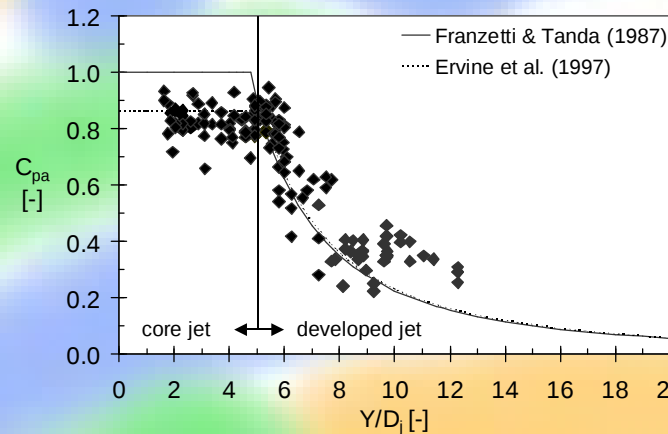


## Plunge pool

- $Y/D_j$  ratio
- centerline mean ( $C_{pa}$ ) and fluctuating ( $C'_{pa}$ ) dynamic pressures

$$C_{pa} = 38.4 \cdot (1 - \alpha_i) \cdot \left( \frac{D_j}{Y} \right)^2 \quad \text{for } Y/D_j > 4-6$$

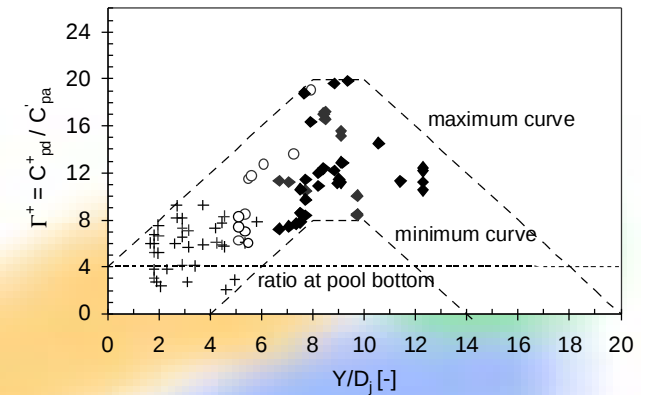
$$C_{pa} = 0.85 \quad \text{for } Y/D_j < 4-6$$



$$C'_{pa} = 0.0022 \cdot \left( \frac{Y}{D_j} \right)^3 - 0.0079 \cdot \left( \frac{Y}{D_j} \right)^2 + 0.0716 \cdot \left( \frac{Y}{D_j} \right) + 0.0583$$

1.) Maximum dynamic pressure  $C_p^{\max}$  in a closed-end joint

$$P_{\max} [\text{Pa}] = \gamma \cdot C_{pd}^{\max} \cdot \frac{\phi \cdot V_j^2}{2g} = \gamma \cdot \underbrace{(C_{pa} + \Gamma^+ \cdot C'_{pa})}_{C_{pd}^+} \cdot \frac{\phi \cdot V_j^2}{2g}$$

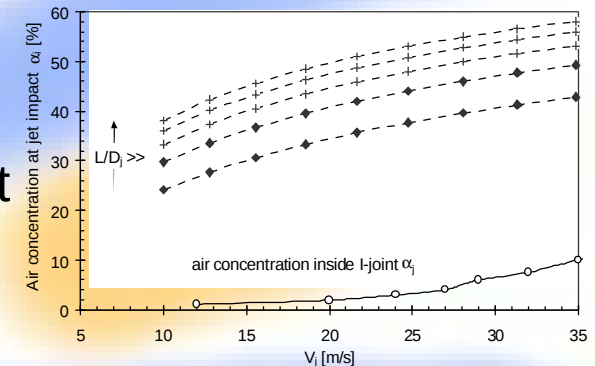


2.) Characteristic amplitude of pressures  $\Delta p_c$  in a closed-end joint

3.) Characteristic frequency of pressures  $f_c$  in a closed-end joint

$$c [\text{m/s}] = 4 \cdot L_j \cdot f_c \sim 100 - 200$$

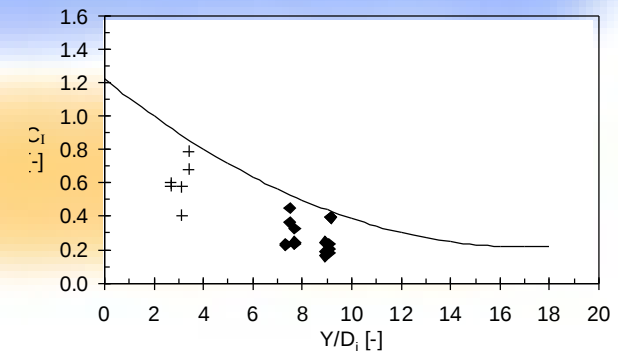
$$f_c [\text{Hz}] \sim 10 - 100$$



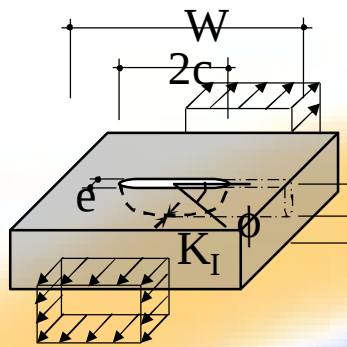
4.) Maximum dynamic impulsion  $C_I^{\max}$  in an open-end joint

$$\left. \begin{array}{l} p_{up} = C_{up} \cdot V^2/2g \\ \Delta t_{up} = T_{up} \cdot 2L/c \end{array} \right\} I_{up} = p_{up} \cdot \Delta t_{up} = C_{up} \cdot T_{up} \cdot (V^2 L / gc) = C_I \cdot (V^2 L / gc) [\text{m.s}]$$

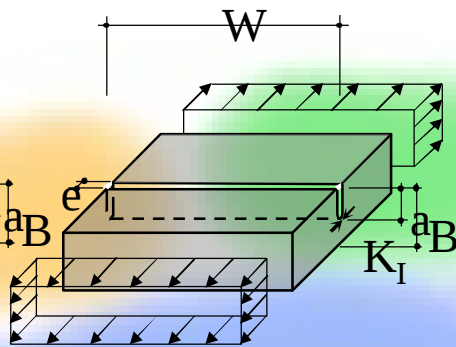
$$C_I = 0.0035 \cdot \left( \frac{Y}{D_j} \right)^2 - 0.119 \cdot \left( \frac{Y}{D_j} \right) + 1.22$$



Semi-elliptical (EL)



Single-edge (SE)



$\sigma_{\text{water}}$

$\sigma_{\text{water}}$

## 1. Stress Intensity at crack tip

$$K_I = C^{\max}_p \sqrt{\pi \cdot a} \cdot f\left(\frac{a}{W}\right)$$

## 2. Fracture toughness of rock

$$K_{I \text{ ins, } T} = A \cdot (1.2 \text{ to } 1.5) \cdot T + (0.054 \cdot \sigma_c) + B$$

$$K_{I \text{ ins, } UCS} = C \cdot (1.2 \text{ to } 1.5) \cdot UCS + (0.054 \cdot \sigma_c) + D$$

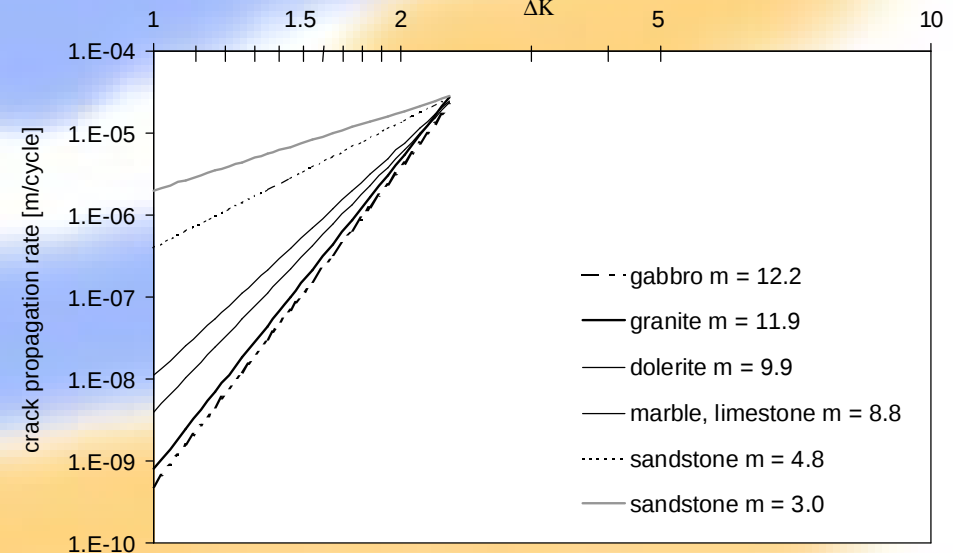
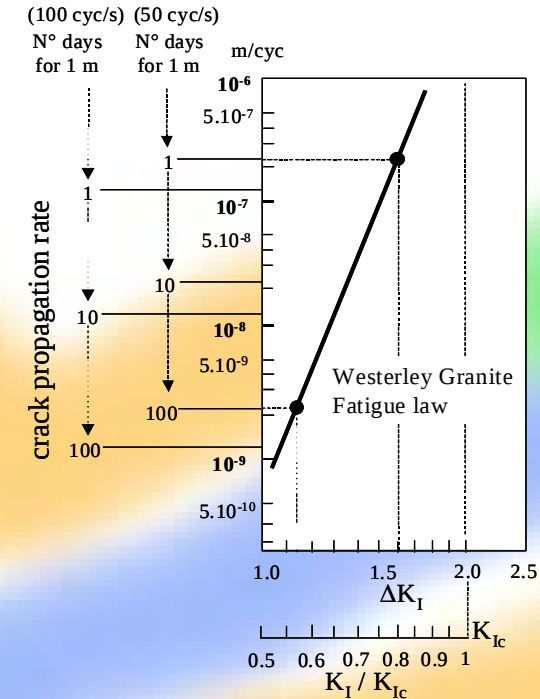
## 3. Instantaneous crack propagation ( $C^{\max}_p$ )

$$K_I > K_{I \text{ ins}}$$

## 4. Time-dependent crack propagation ( $\Delta p_c, f_c$ )

$$K_I < K_{I \text{ ins}}$$

$$\frac{da}{dN} = C_r \cdot (\Delta K_I)^{m_r}$$

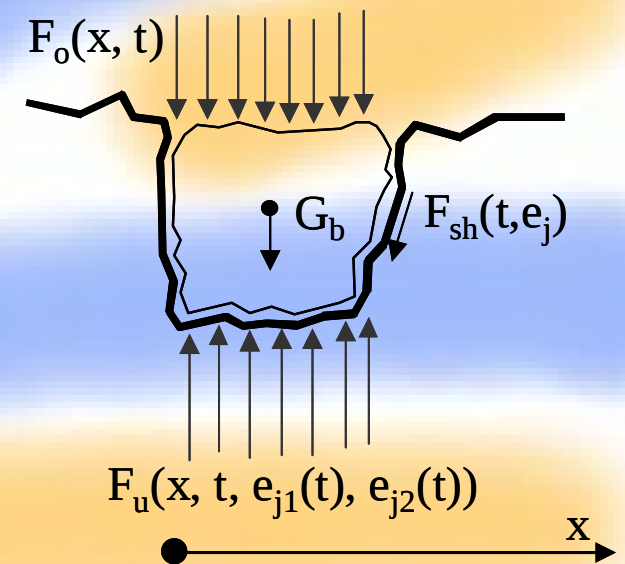
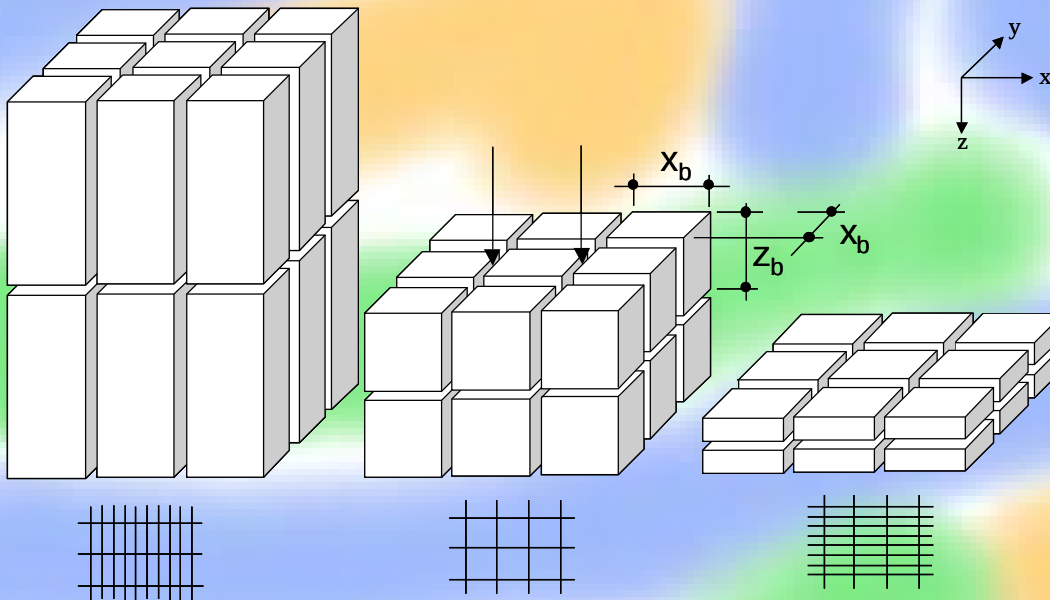


$$I_{\Delta\text{pulse}} = \int_0^{\Delta\text{pulse}} (F_u - F_o - G_b - F_{sh}) \cdot dt = m \cdot V_{\Delta\text{pulse}}$$

|          |   |                               |
|----------|---|-------------------------------|
| $F_u$    | = | underpressures                |
| $F_o$    | = | overpressures                 |
| $G_b$    | = | weight of rock block          |
| $F_{sh}$ | = | shear and interlocking forces |

$$G_b = \nabla \cdot (\gamma_r - \gamma_w) = x_b^2 \cdot z_b \cdot (\gamma_r - \gamma_w)$$

$$V_{\Delta\text{pulse}} = \sqrt{2 \cdot g \cdot h_{up}}$$



# Tucuruí Dam plunge pool (Brazil)

## Tocantins-Araguaia basin

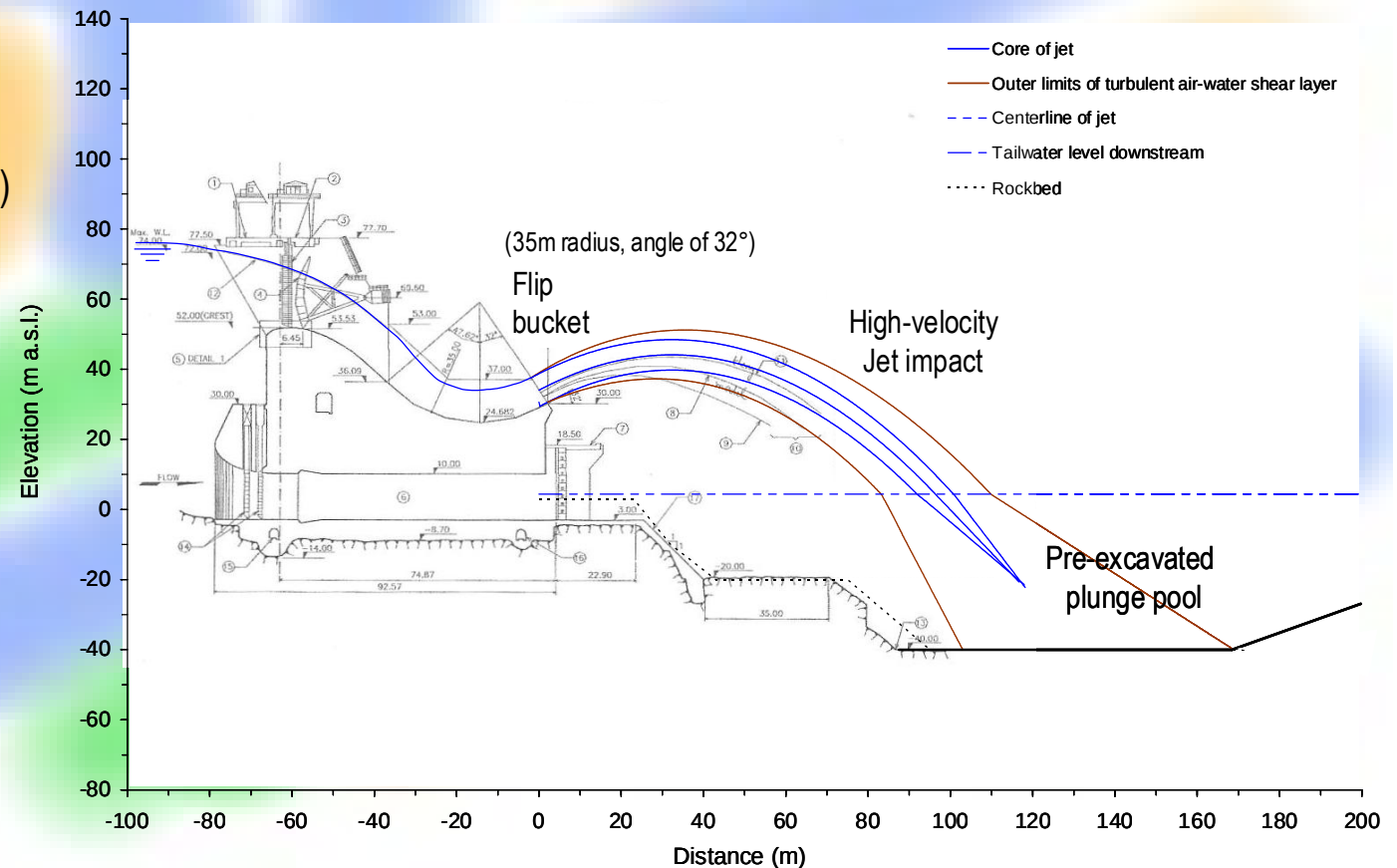
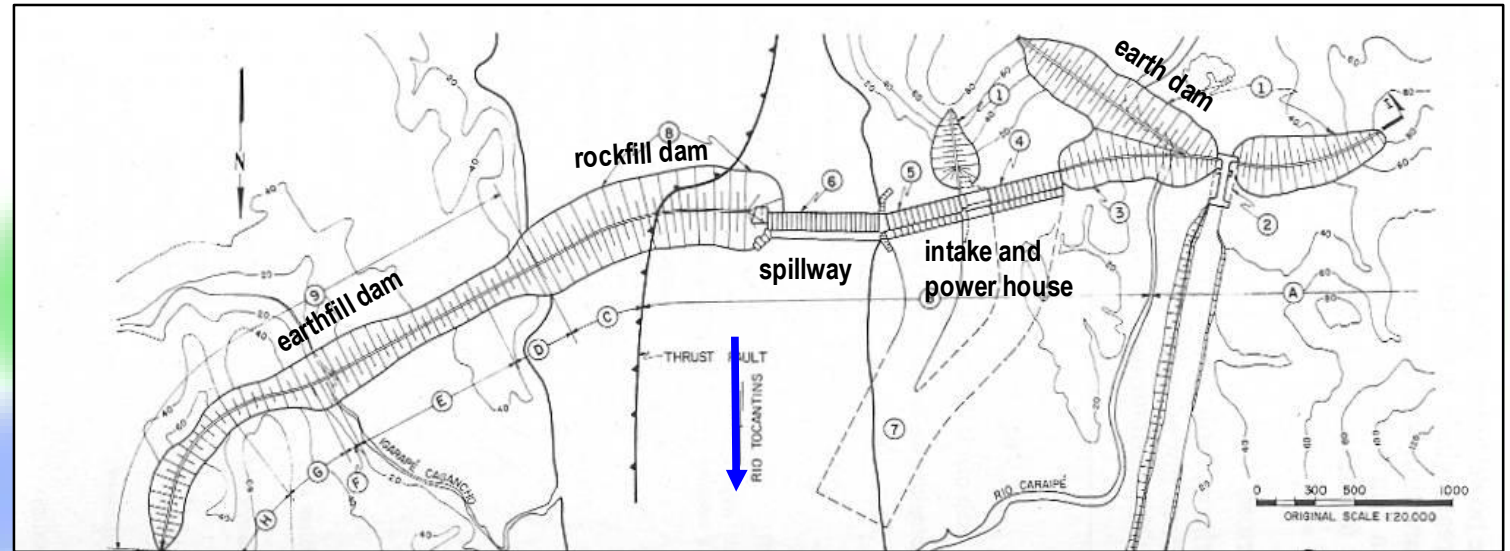
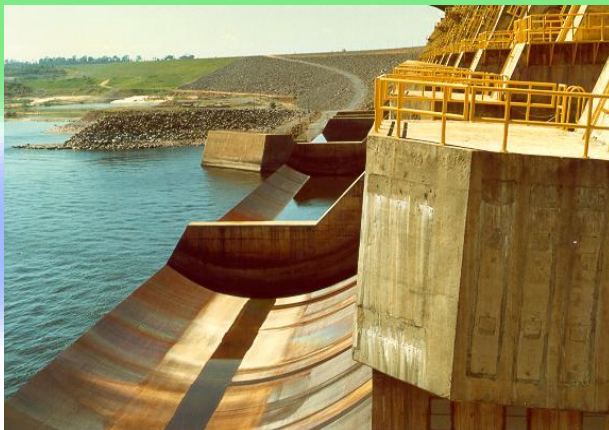


- catchment area Tocantins River 758'000 km<sup>2</sup> (7.5 % of land mass of Brazil)
- Tocantins River has a total length of 2'500 km
- average annual flow rate of 10'900 cms
- dry season in September-October
- peak flooding during February-April (average monthly flows of 50'000 cms)

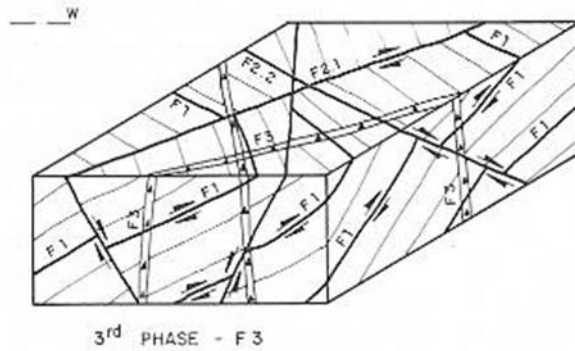
# Tucurui Dam plunge pool (Brazil)

## Tucurui Dam Complex

- 86 m high rockfill dam on Tocantins River
- 6'900 m long main dam wall
- meta-sedimentary rock at spillway
- 2<sup>nd</sup> largest spillway worldwide (110'000 m<sup>3</sup>/s)
- pre-excavated plunge pool at - 40 m
- almost no scour since dam construction
- 23 rectangular gates 21 m x 20 m wide
- floods during 3 months / year (Feb-April)

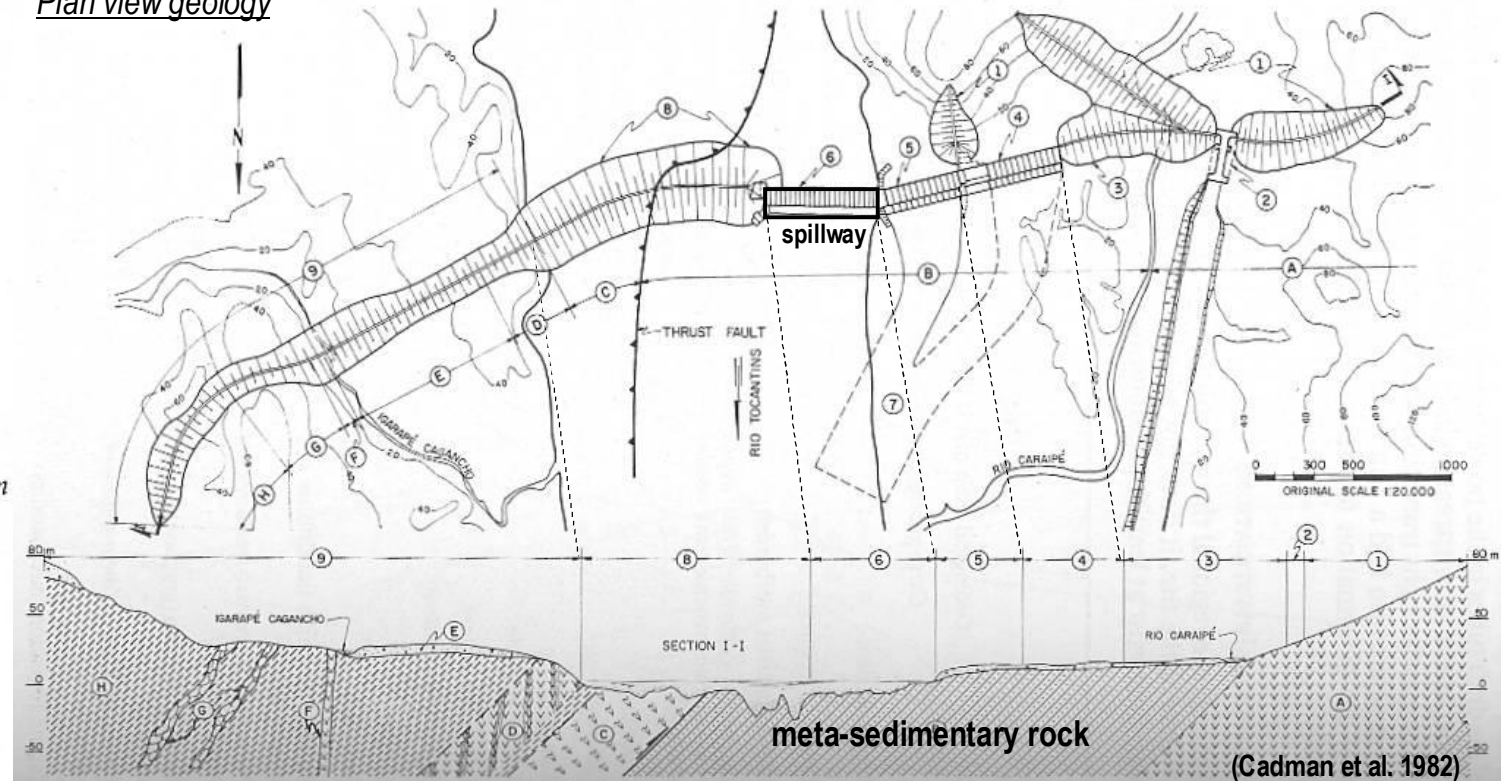


## Fault structures



- F 1 Thrust faults parallel to bedding  
*Failles inverses parallèles à la stratification*
- F 2.1 Normal faults dipping west  
*Failles normales plongeant vers l'ouest*
- F 2.2 Normal faults dipping south  
*Failles normales plongeant vers le sud*
- F 2.3 Normal faults dipping east  
*Failles normales plongeant vers l'est*
- F 3 Strike — slip subvertical faults  
*Failles transcourantes sub-verticales*

## Plan view geology

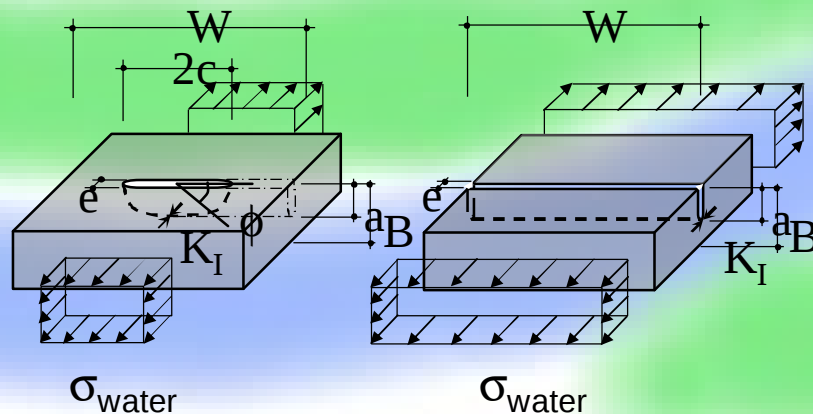


## Meta-sedimentary rock

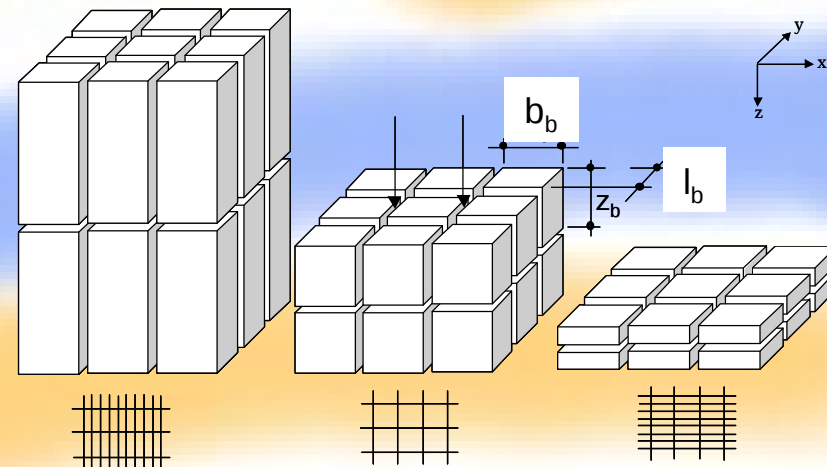
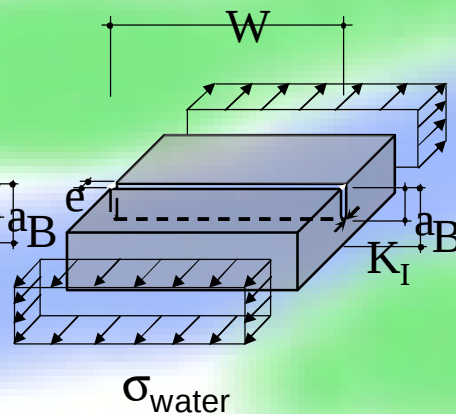
- Unconfined Compressive Strength of intact rock = ~ 125 MPa
- multiple families of faults, joints
- one major fault through the center of the riverbed
- very complex situation (lithology – tectonic structure – faults)
- near-horizontal bedding, sliding stability

| Property                           | Symbol     | CONSERV     | AVERAGE    | BENEF    | Unity             |
|------------------------------------|------------|-------------|------------|----------|-------------------|
| Unconfined Compressive Strength    | UCS        | 50          | 75         | 125      | MPa               |
| Density rock                       | $\gamma_r$ | 2600        | 2700       | 2800     | kg/m <sup>3</sup> |
| Ratio horizontal/vertical stresses | $K_0$      | 2-3         | 2-3        | 2-3      | -                 |
| Typical maximum joint length       | L          | 1           | 1          | 1        | m                 |
| Vertical persistence of joint      | P          | 0.25        | 0.25       | 0.25     | -                 |
| Form of rock joint                 | -          | single-edge | elliptical | circular | -                 |
| Tightness of joints                | -          | tight       | tight      | tight    | -                 |
| Total number of joint sets         | $N_j$      | 3+          | 3          | 2+       | -                 |
| Typical rock block length          | $l_b$      | 1           | 1          | 1        | m                 |
| Typical rock block width           | $b_b$      | 1           | 1          | 1        | m                 |
| Typical rock block height          | $z_b$      | 0.5         | 0.75       | 1        | m                 |
| Joint wave celerity                | c          | 150         | 125        | 100      | m/s               |
| Fatigue sensibility                | m          | 8           | 9          | 10       | -                 |
| Fatigue coefficient                | C          | 1.00E-07    | 1.00E-07   | 1.00E-07 | -                 |

Semi-elliptical (EL)  
Circular (C)



Single-edge (SE)



# Flooding and bathymetric surveys (1969-2001)

## Flooding survey (available since 1969)

- 1969 – 1980: statistical analysis based on Tucuruí and Itupiranga about 175 km upstream, PMF = 90'000 cms
- 1978-1980: 3 major flood events during dam construction, up to 68'000 cms
- 1980-present: more detailed flood analysis, PMF = 110'000 cms, somewhat conservative, maximum peak since dam construction = 43'000 cms (Jan 1990)

## Bathymetric survey

### Survey 1 (1984)

Sedimentation along right hand side of plunge pool due to 3 yrs of river diversion during dam construction

### Survey 2 (1985)

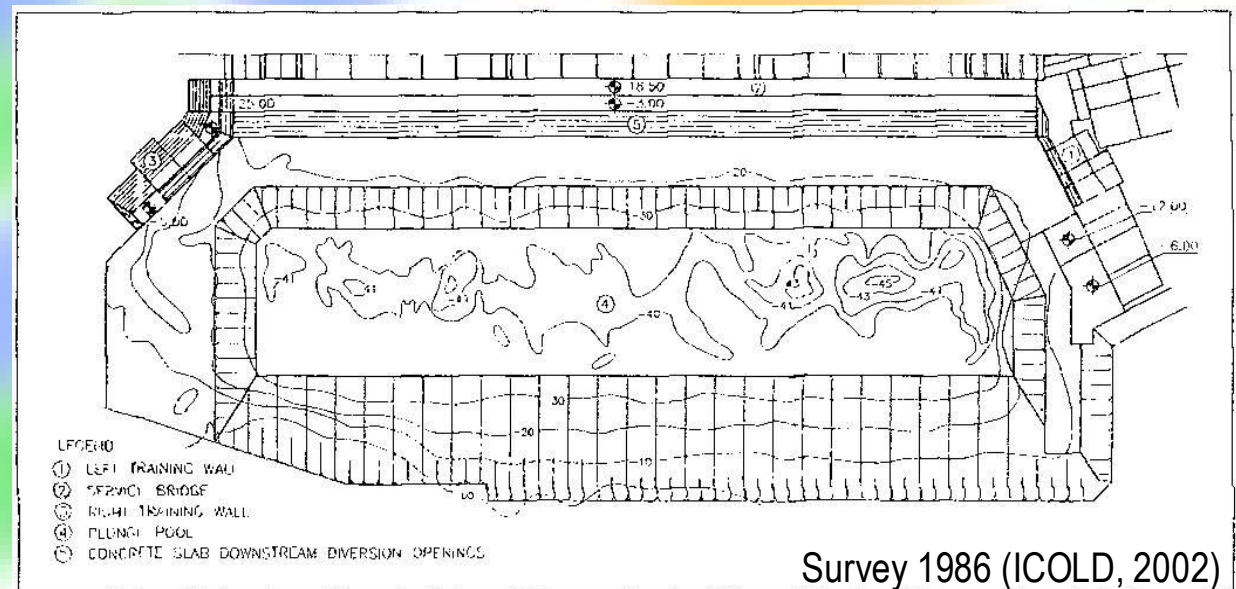
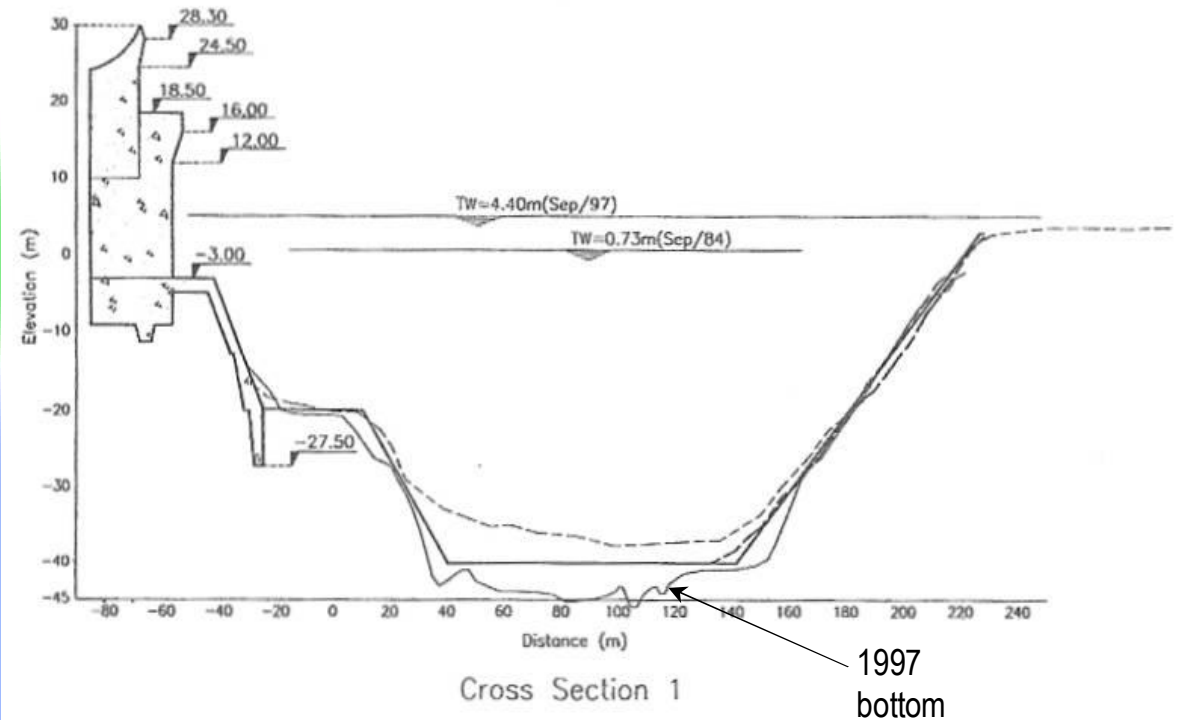
No specific issues, only left hand side of basin has been surveyed due to strong turbulent vortices

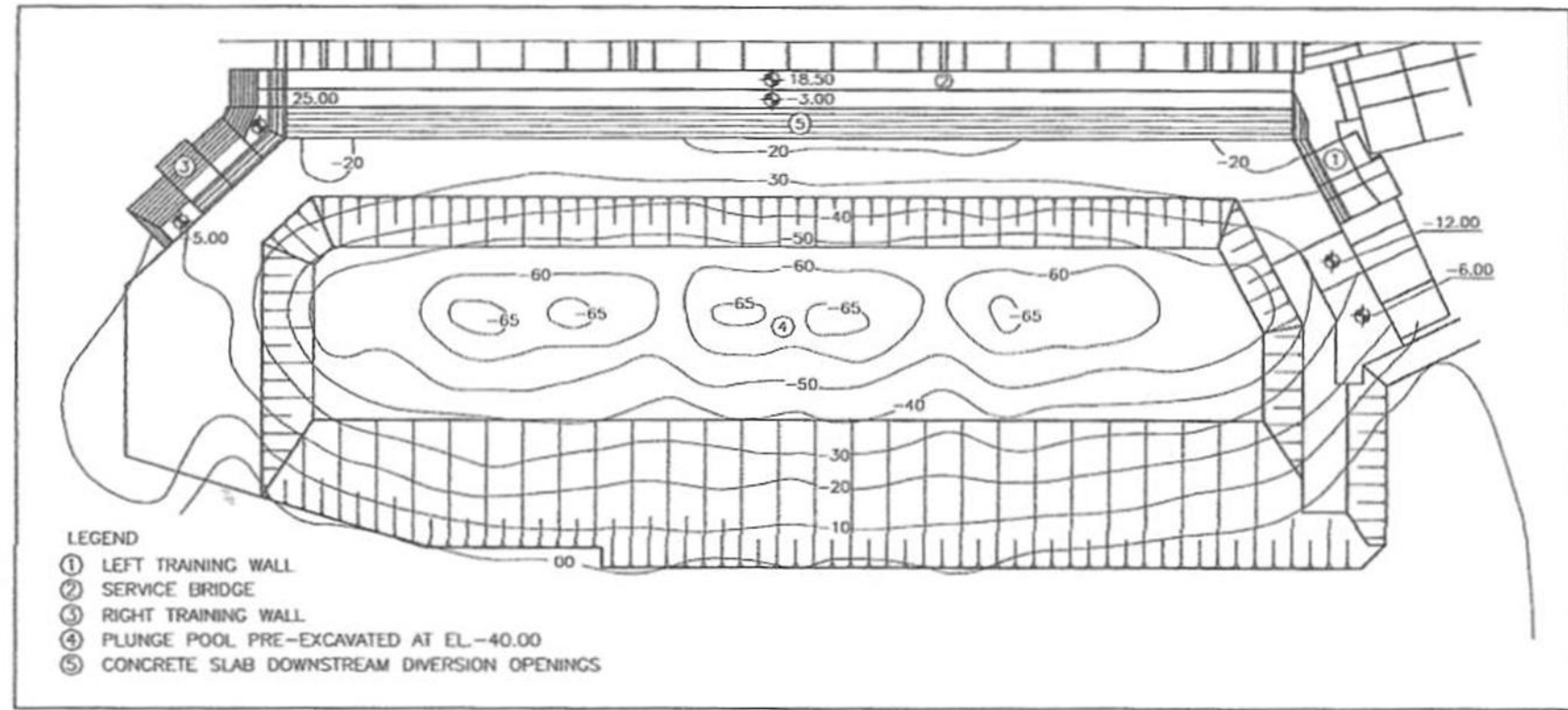
### Survey 3 (1986)

Former sediment deposits washed away. Slight erosion (max. 5 m) along two local areas of plunge pool bottom and probably related to removal of partially detached (blasting) rock blocks.

### Survey 4 (1997)

Same erosion in same areas as found during the 1986 survey. No specific issues to notice.





**Figure 1.-** Scour formation in plunge pool following laboratory test with gravel and 100'000 cms (Large Brazilian Spillways, ICOLD, Petry et al., 2002)

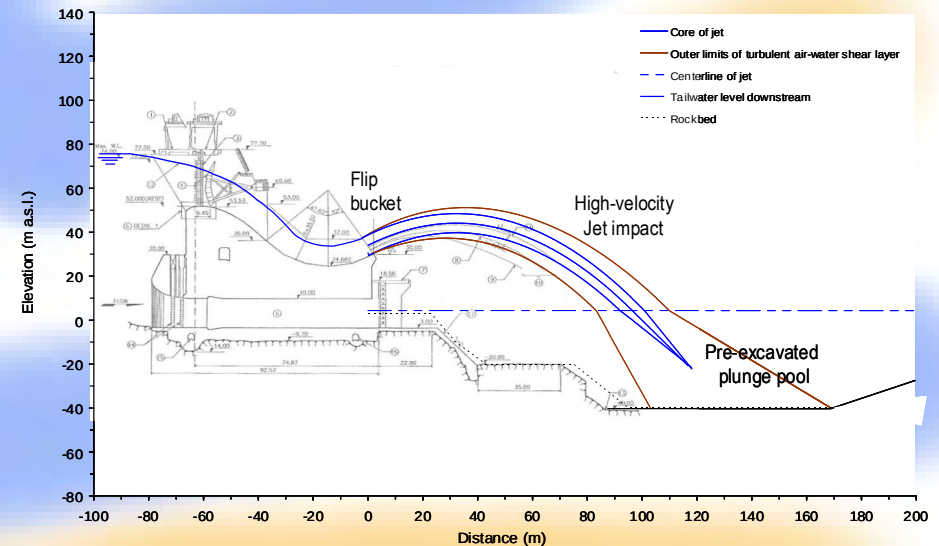
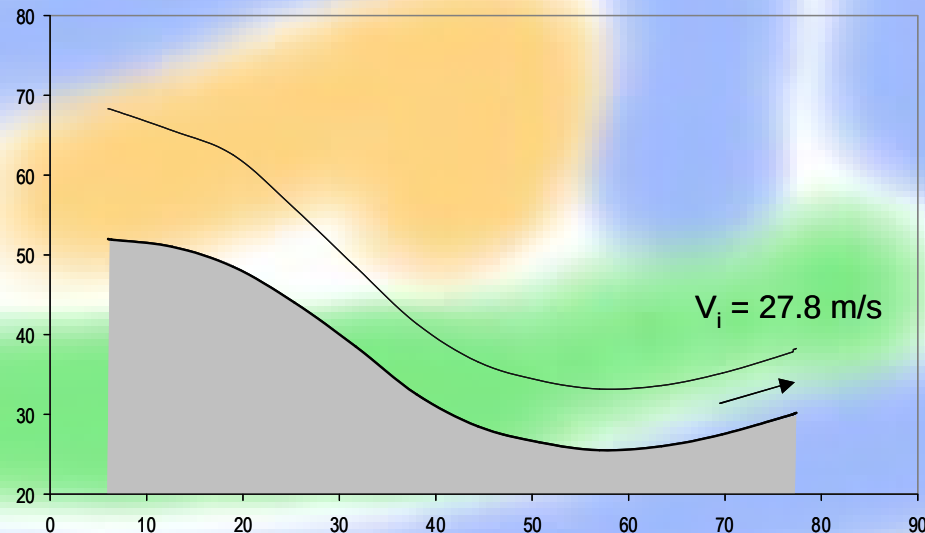
- discharges between 15'000 and 100'000 cms
- plunge pool bottoms at elevations of -15m, -25m, -40m
- pool at -40m:
  - no erosion for discharges of up to 50'000 cms (calibration model)
  - erosion until - 65m for discharge of 100'000 cms

## Falling jet at Tucurui Dam

The jet at Tucurui Dam is issuing from a chute with flip bucket. As such, numerical computations have first been performed of the air-water flow characteristics along the chute. The water surface line for a  $110'000 \text{ m}^3/\text{s}$  is presented in Figure 4.

The flow velocity at the lip of the flip bucket equals  $27.8 \text{ m/s}$ , for a total flow depth of about  $8 \text{ m}$ . The upstream water level is  $75.3 \text{ m a.s.l.}$  and the downstream plunge pool water level is at  $4.4 \text{ m a.s.l.}$  The jet is thus of rectangular shape with a width of  $20\text{m}$  and an issuance thickness of  $8\text{m}$ .

Second, the jet characteristics at impact in the tailwater depth have been defined based on ballistics accounting for air drag. As such, the jet velocity at impact has been computed at  $37.9 \text{ m/s}$  for an inner jet core diameter of about  $6.9 \text{ m}$ . Its turbulence intensity has been estimated at  $8 \%$  and its air concentration at impact at  $40 \%$ , corresponding to very turbulent air-water jets.



## Plunge pool diffusion at Tucurui Dam

The diffusion of the jet through the pool water depth is presented in Figure 2. Significant spread of the jet is computed, with an outer jet diameter at impact in the pool of about  $20\text{m}$ . The jet core vanishes before impacting the plunge pool bottom, corresponding to fully developed jet conditions.

# Application of Comprehensive Scour Model

## Results of computations

**Table 2a.-** Scour elevations as a function of time duration of flood following a 100'000 m<sup>3</sup>/s flood event at Tucurui Dam (CSM model)

| SCOUR ELEVATION COMPUTATIONS |      |        |       |       |       |       |       |       |       |
|------------------------------|------|--------|-------|-------|-------|-------|-------|-------|-------|
| TIME                         |      |        |       | CFM   |       |       | DI    |       |       |
| Hours                        | Days | Months | Years | BENEF | AVER  | CONS  | CONS  | AVER  | BENEF |
| 96                           | 4    | 0.1    | 0.01  | -40.4 | -53.6 | -61.6 | -93.9 | -78.9 | -63.2 |
| 192                          | 8    | 0.3    | 0.02  | -40.4 | -53.6 | -62.6 | -93.9 | -78.9 | -63.2 |
| 720                          | 30   | 1.0    | 0.08  | -40.4 | -54.3 | -64.1 | -93.9 | -78.9 | -63.2 |
| 1500                         | 62.5 | 2.1    | 0.17  | -40.4 | -54.9 | -65.0 | -93.9 | -78.9 | -63.2 |
| 5760                         | 240  | 8.0    | 0.67  | -40.4 | -56.4 | -67.2 | -93.9 | -78.9 | -63.2 |
| 57600                        | 2400 | 80.0   | 6.67  | -42.6 | -59.2 | -74.3 | -93.9 | -78.9 | -63.2 |

**Table 2b.-** Scour elevations as a function of time duration of flood following a 50'000 m<sup>3</sup>/s flood event at Tucurui Dam (CSM model)

| SCOUR ELEVATION COMPUTATIONS |      |        |       |       |       |       |       |       |       |
|------------------------------|------|--------|-------|-------|-------|-------|-------|-------|-------|
| TIME                         |      |        |       | CFM   |       |       | DI    |       |       |
| Hours                        | Days | Months | Years | BENEF | AVER  | CONS  | CONS  | AVER  | BENEF |
| 96                           | 4    | 0.1    | 0.01  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |
| 192                          | 8    | 0.3    | 0.02  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |
| 720                          | 30   | 1.0    | 0.08  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |
| 1500                         | 62.5 | 2.1    | 0.17  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |
| 5760                         | 240  | 8.0    | 0.67  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |
| 57600                        | 2400 | 80.0   | 6.67  | -40.6 | -40.6 | -40.6 | -45.1 | -40.0 | -40.0 |

## Conclusions

1. Almost no scour formation for 100'000 cms and under beneficial parametric assumptions
2. Small scour forms under average parametric assumptions and for 100'000 cms (10m of scour formation)
3. The laboratory model tests are probably somewhat on the conservative side (25m of socur formation)
4. For a completely broken up rock mass (detached blocks with depth), significant scour would form, however not plausible